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## STANDARD DEFINITIONS FOR NUMERICAL SOLUTION OF HEAT TRANSPORT EQUATIONS

Notations:

a) Diffusion coefficients:

Electrons:  $\chi_e$

Ions:  $\chi_{ion}$  (The sum over ion species:  $n_i \chi_i$  is written  $NION \chi_{ion}$ )

$NION = NM1 + NM2 + NIMP$  (Note: includes impurities, excludes fast ions)

b) Convection term:

Electrons: Flow multiplication factor:  $\gamma_e$  (usually set equal to 3/2)

Convection source term:  $C_e$  (usually set equal to 0)

Ions: Flow multiplication factor:  $\gamma_{ion}$  (usually set equal to 3/2)

Convection source term:  $C_{ion}$  (usually set equal to 0)

c) Boundary conditions:

In the following, the variable TE and TI (in eV) are determined self-consistently as solution of the diffusion equations (6) and (7) using as boundary condition the measured **TE** and **TI** at  $\rho = 0.9$ .

d) Source terms:

2) Volume differential:

$$V' = (\text{VOLUME}) / \rho$$

3) Electron particle flow is defined as a solution of:

$$\frac{1}{\rho} \Gamma_e = V' [\text{SNBIE} + \text{PGASZ} * \text{SWALL} - \text{DNER}]$$

4) Simplified ion particle flow:

$$\Gamma_{ion} = \Gamma_e / \text{PGASZ}$$

5) Equipartition coupling coefficient :

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(from NRL Handbook simplified for  $m_e \ll m_i$ ):

$$Q_{ei} = \frac{3}{2} \text{NE} \alpha_{ei} k [T_e - T_i]$$

$$\alpha_{ei} = 3.169 \cdot 10^{-15} \ln(\Lambda) \frac{1}{T_e^{3/2}} \left[ \frac{\text{PGASZ}^2}{\text{PGASA}} \text{NM1} + \frac{\text{BGASZ}^2}{\text{BGASA}} \text{NM2} + \frac{\text{PIMPZ}^2}{\text{PIMPA}} \text{NIMP} \right]$$

$$\ln(\Lambda) = 30.908 - \ln\left(\frac{\text{NE}^{1/2}}{T_e}\right)$$

$$k = 1.6 \cdot 10^{-19}$$

6) Electron heat transport equations:

a) Heat source terms:

$$Q_e = \text{QNBIE} + \text{QICRHE} + \text{QECHE} + \text{QLHE} + \text{QIBWE} + \text{QOHM} + \text{QFUSE} \\ - \text{QWALLE} - \text{QGRAD}$$

b) Diffusion equation:

$$-\frac{1}{\rho} \left[ -V' \text{GRHO2} \text{NE} \chi_e \frac{1}{\rho} T_e + \gamma_e \Gamma_e T_e \right] = V \left[ -\text{NE} T_e C_e - Q_{ei} + Q_e - \text{DWER} \right]$$

7) Ion heat transport equation:

a) Heat source terms:

$$Q_{ion} = \text{QNBII} + \text{QICRHI} + \text{QECHI} + \text{QLHI} + \text{QIBWI} + \text{QFUSI} \\ - \text{QWALLI}$$

b) Diffusion equation (summed over all ion species):

$$-\frac{1}{\rho} \left[ -V' \text{GRHO2} \text{NION} \chi_{ion} \frac{1}{\rho} T_i + \gamma_{ion} \Gamma_{ion} T_i \right] = \\ V \left[ \text{NION} C_{ion} T_i + Q_{ei} + Q_{ion} - \text{DWIR} \right]$$